

# COMPLEX NUMBER SYSTEMS & OPERATIONS

Advanced Mathematics Reference Sheet

## Fundamental Representations

Rectangular  $z = a + bi$

Polar  $z = r(\cos \theta + i \sin \theta)$

Exponential  $z = re^{i\theta}$

## Conversion Constants

Modulus ( $r$ )  $|z| = \sqrt{a^2 + b^2}$

Argument ( $\theta$ )  $\theta = \tan^{-1}(b/a)$

Conjugate ( $\bar{z}$ )  $a - bi$

## Advanced Theorems & Identities

### Euler's Identity

$$e^{i\pi} + 1 = 0$$

### De Moivre's Theorem

$$[r(\cos \theta + i \sin \theta)]^n = r^n (\cos n\theta + i \sin n\theta)$$

## Complex Functions & Calculus

### Operation

### Definition / Identity

Complex Logarithm  $\ln(z) = \ln|z| + i(\arg z + 2k\pi)$

n-th Roots  $w_k = \sqrt[n]{r} [\cos((\theta + 2k\pi)/n) + i \sin((\theta + 2k\pi)/n)]$

Hyperbolic Relation  $\sin(iz) = i \sinh(z) \mid \cos(iz) = \cosh(z)$

## Geometric Interpretation (Argand Diagram)

[ Plot Area: Horizontal Axis (Re) / Vertical Axis (Im) ]  
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