

COMPLEX NUMBERS REFERENCE

ADVANCED ALGEBRA QUICK-STUDY GUIDE

The Imaginary Unit

$$i = \sqrt{-1}$$

$$i^2 = -1$$

$$i^3 = -i$$

$$i^4 = 1$$

Standard Form

$$z = a + bi$$

Where **a** is the real part (Re) and **bi** is the imaginary part (Im).

Fundamental Operations

Operation	Definition / Formula
Addition	$(a + bi) + (c + di) = (a + c) + (b + d)i$
Subtraction	$(a + bi) - (c + di) = (a - c) + (b - d)i$
Multiplication	$(a + bi)(c + di) = (ac - bd) + (ad + bc)i$
Conjugate	$z = a + bi \quad \bar{z} = a - bi$
Division	Multiply numerator and denominator by \bar{z} ...

Absolute Value (Modulus)

$$|z| = \sqrt{a^2 + b^2}$$

Polar Form

$$z = r(\cos \hat{I} + i \sin \hat{I})$$

$$r = |z|, \hat{I} = \tan^{-1}(b/a)$$

EULER'S FORMULA

$$e^{i\hat{I}} = \cos \hat{I} + i \sin \hat{I}$$